Time nT (N-1) T Frequency fNT 0  $\vec{\mathbf{W}}_{m-1}$ **₩**<sub>2</sub> **™ \*** 

FIG. 1 Wavelet Tiling of an N-Point Digital t-f Space

Wavelet Iterated Filter Bank for Tiling t-f Space in FIG. FIG. 2

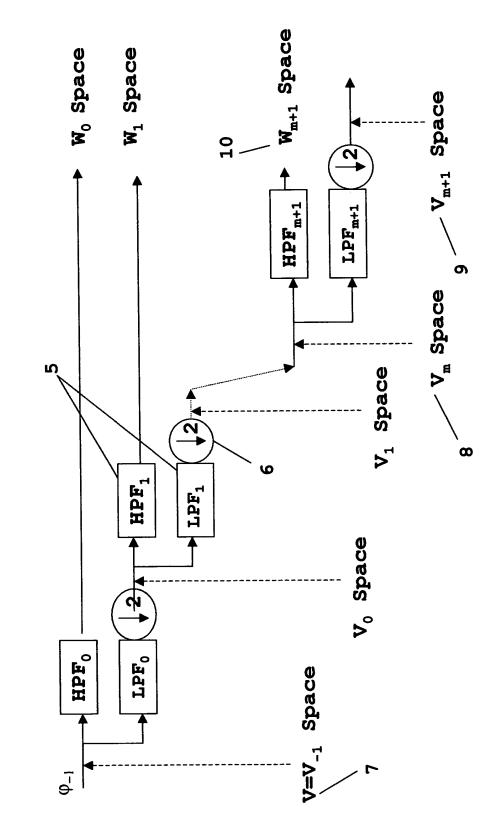
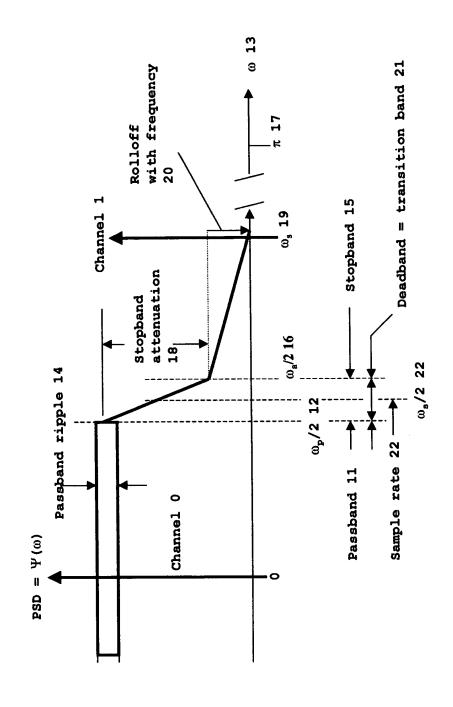
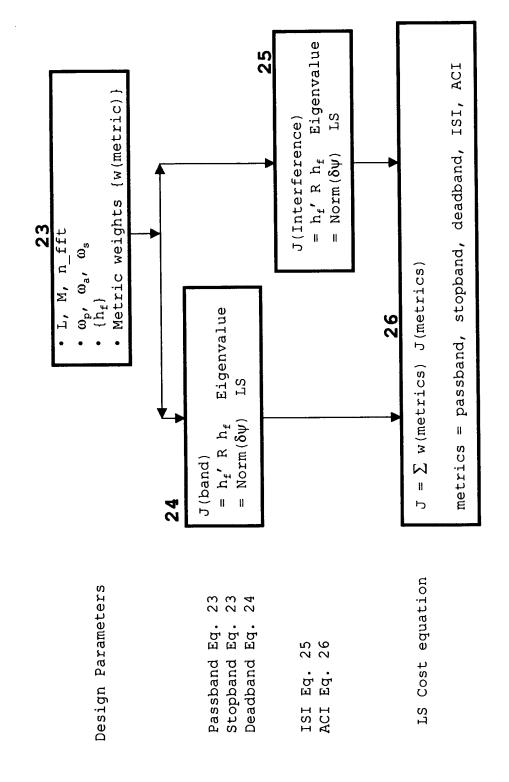


FIG. 3 PSD Requirements for Communications



LS Metrics and Cost Function FIG.



## FIG. 5A LS RECURSIVE DESIGN ALGORITHM IN MATLAB 5.0 CODE TO DESIGN:

- MOTHER WAVELET IN FIG. 6
- NEW WAVELET FROM MOTHER WAVELET

```
Σ
                                                                                                                                                                                                                                                                        0
                                                                                                                        nominal Wavelet length in units of
                                                                                                                                                                                                                                                                                                                   maximum number of channels allowed
                                                                                                                                                                                                                                                                                                                                                                                                                                                                  % number of iterations for LS design
                                                                                                                                                                                                                                                                                                                                                   % wp/2pi edge of passband
% ws/2pi edge of stopband
                                                                                                                                                                                                                      FFT size for spectrum centered at
                                                                                                                                                                        = normalized Wavelet sample rate
                                                                                                                                                                                                                                                      dB, channel-to-channel imbalance
                                                                                                                                                                                         normalized channel passband
                                                                                                                                                         normalized channel spacing
                                                                                                                                                                                                         number of design harmonics
                                                                                                                                                                                                                                                                                                                                                                                  edge of passband
                                                                                                                                                                                                                                                                                                                                                                                                   edge of stopband
                                                                                                                                                                                                                                                                                                                                     % 0.5 * Wavelet sample rate
- PERFORMANCE DATA AND PLOTS
                                                                                                          % Wavelet sample interval
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   weighting for passband
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   stopband
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  weighting for deadband
                                                                                                                                          Wavelet length N =ML+1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   weighting for ISI
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  weighting for ACI
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   weighting for
                                                                                                                                                                                                                                                                                                     % definition
                                                                                                                                                                                                                                       dB, Eb/No
                                                                                                                                                                                                                                                                                                                                                                                                                                     % STEP 1.3 OPTIMIZATION PARAMETERS
                                                                                                                                                                                                                                                                                                                                                                                  floor(f_pass*n_fft)
floor(f_stop*n_fft)
                                            & STEP 1 DESIGN PARAMETERS
                                                                             % STEP 1.1 SCENARIO PARAMETERS
                                                                                                                                                                                                                                                                                       & STEP 1.2 DERIVED PARAMETERS
                                                                                                                                                                                                                                                                                                                                                                     = (2-fp)/(M*fs)
                                                                                                                                                                                                                                                                                                                                     = (n_fft/M)
                                                                                                                                                                                                                                                                                                                                                   = fp/(M*fs)
                                                                                                                                                                                         0.8864;
                                                                                                                                                                                                                                                                                                       = pi^*2;
                                                                                                                                                                                                                        = 1024;
                                                                                                                                                                                                                                       = 6.0 ;
= 6.0 ;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     2.e-3
                                                                                                                                             = M*L+1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     = 1.e-2
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    = 0.80
                                                                                                                                                                                                                                                                                                                                                                                                                                                                     n iteration = 10;
                                                                                                            = 1.6;
                                                                                                                            = 16;
                                                                                                                                                                                                         = 16
                                                                                                                                                                                                                                                                                                                                                                                                                         11
                                                                                                                                                                                                                                                          x_imbal_aci
                                                                                                                                                                                                                                                                                                                                                                                 nfft_pass
                                                                                                                                                                                                                                                                                                                                                                                                     nfft_stop
                                                                                                                                                                                                                                                                                                                                       nfft wsr
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     alpha_4
alpha_5
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      alpha_1
alpha_2
alpha_3
                                                                                                                                                                                                                                                                                                                                                      f_pass
f_stop
                                                                                                                                                                                           fp
n_f
n_fft
                                                                                                                                                                                                                                                                                                         twopi
                                                                                                                                                                                                                                            epno
                                                                                                                                                             Ęs
```

#### FIG. 5B

```
STEP 2.4 MATRIX "c matrix" USED FOR ISI, ACI LS ERROR METRICS J(ISI) IN EQ. 25 AND J(ACI) IN EQ. 26
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  b_{\mathsf{w}} \max(1,:) = \operatorname{ones}(1,\mathbf{n}_{\mathsf{f}});
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   EQ. 23 AND FUNCTION "pmn_d" CACULATES ERROR MATRIX FOR J(DEAD) IN EQ. 24
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       STEP 2.3 FUNCTION "pmn" CALCULATES PASSBAND, STOPBAND LS ERROR MATRICES FOR THE METRICS J(PASS), J(STOP) IN
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   & STEP 2.5 PASSBAND, STOPBAND, WAVELET SAMPLE RATE TEMPLATES
                                                                                                                                                                                                                                                                                                                                                                                       8 STEP 2.2 MATRIX "bw matrix" MAPS WAVELET FREQUENCY DESIGN
8 HARMONICS INTO WAVELET TIME RESPONSE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                        bw_matrix = zeros(m,n_f);
for 1_r=1:m
    ang = 2*p1* rem( (i_r)*(0:n_f-1)/(N-1),1); % time
bw_matrix(i_r + 1, :) = 2 * cos(ang);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       v_1 = 1:nfft_pass+1;
v_2 = nfft_pass+2:nfft_stop;
v_3 = nfft_stop+1:nfft_stop+nfft_pass;
hw_ref= [zeros(size(v_1)) -110*ones(size(v_2)) ...
zeros(size(v_3))];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     %===set up wavelet sample rate templet
v_lb = 1:nfft wsr;
v_2b = nfft_wsr+1:nfft_wsr+1;
v_3b = nfft_wsr+2:nfft_wsr+nfft_pass+nfft_stop;
hw_wsr= [-110*ones(size(v_lb)) zeros(size(v_2b))
& STEP 2 INITIALIZATION CALCULATIONS
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               seeset up passband and stopband templet
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    c matrix=[bb; flipud(bb(1:m,1:(m+1)))]/2;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 au=eye(m+1,m+1); % identity matrix
                                                              STEP 2.1 WAVELET LENGTH PARAMETERS
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 _matrix(m+1,1)=c_matrix(m+1,1)*2;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              % rotation
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       -110*ones(size(v_3b))];
                                                                                                                                                                                                                                                                                    N is even
                                                                                                                 nodd= fix( N/2 );
nodd = N - 2 * nodd ;
if ( nodd == 1)
m = (N - 1 ) /2 %
                                                                                                                                                                                                                                                                                       æ
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   bb=rot90(au);
                                                                                                                                                                                                                                                                                       m = N/2;
                                                                                                                                                                                                                                    nrow = m+1;
                                                                                                                                                                                                                                                                                                                   nrow = m;
                                                                                                                                                                                                                                                                                                                                              end
```

#### FIG. 5C

# % STEP 3 PASSBAND, STOPBAND, DEADBAND LS ERROR MATRICES

```
STEP 3.4 WEIGHTED LS ERROR MATRIX "P_total" FOR THE WEIGHTED SUM OF J(PASSBAND), J(STOPBAND), J(DEADBAND)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     p_total= alpha_1*passband+alpha_2*stopband+alpha_5*deadband;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           STEP 3.5 CONVERT IS ERROR MATRIX IN TIME "p_total" TO LS ERROR MATRIX IN FREQUENCY "pw_t"
% STEP 3.1 J(PASSBAND) LS ERROR MATRIX "passband"
                                                                                                                                                                                                % STEP 3.2 J(STOPBAND) LS ERROR MATRIX "stopband"
                                                                                                                                                                                                                                                                                                                                                                                                    % STEP 3.3 J(DEADBAND) LS ERROR MATRIX "deadband"
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   %deadband = pmn_d( omega_1, omega_u, N, an) ;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  pw_total = bw_matrix'*(p_total*bw_matrix);
                                                                                                                                                                                                                                                                                                                                                 stopband = pmn( omega_1, omega_u, N, an) ;
                                                                                                                                          passband = pmn( omega_1, omega_u, N, an);
                                                                                    omega_u = f_pass * pi ; % 0.0554
an=ones(1,nrow);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  deadband = zeros(nrow,nrow);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                 omega_l = f_pass * pi;
omega_u = f_stop * pi;
                                                                                                                                                                                                                                                                                                                                                                                      8------
                                                                                                                                                                                                                                                          omega_l = f_stop * pi;
omega_u = pi ;
                                                            omega_1 = 0.0 * pi;
                                                                                                                                                                                                                                                                                                                         an=zeros(1, nrow);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  pw_t = pw_total;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            an=ones (1, nrow);
```

#### 32

## & STEP 4 ITERATIVE EIGENVALUE SOLUTION

#### FIG. 5D

```
% STEP 4.1 FOR EACH ITERATION "i_iteration" FIND EIGENVECTOR
% IN FREQUENCY THAT MINIMIZES THE COST FUNCTION J IN
EQ. 27 WHOSE LS ERROR MATRIOX IS "pw_t"
xstop = max(hw_db(nfft_stop+1:nfft_stop+nfft_pass+1) );
                                                                                                                                                                                                                              - WAVELET FREQUENCY DESIGN HARMONICS "hw_eig"
- WAVELET IMPULSE RESPONE IN TIME "hn"
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             scale ww = 1. / (hmax^2); \$ normalized hn is the normalized Wavelet response
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              &Fourier transform of hn & hn in the next channel
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    b_vector = bw_matrix * eig_vec(:,min_index);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 %===== peak to_peak ripple in passband
max_ripple = max( hw_db(1: nfft_pass+1));
min_ripple = min( hw_db(1: nfft_pass+1));
xripple = max_ripple - min_ripple ;
%=== stopband atttenuation
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       & STEP 4.3 PASSBAND RIPPLE "xripple" AND & STOPBAND ATTENUATION "xstop"
                                                                                                                eig_val = eig(pw_t);
[eig_vec eigval] = eig(pw_t);
[eigval_min,min_index] = min(eig_val);
                                                                                                                                                                                                                                                                                                                                                                                                                                               hn(1:m) = 0.5*b vector((m+1):-1:2);
hn(m+1) = b vector(1);
hn(m+2:N) = hn(m:-1:1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                hn(m:-1:1) = 0.5 * b_vector(1:m);
                                                                                                                                                                                       hw eig = eig_vec(:,min_index);
hw eig(1) = 2*hw eig(1);
hw max = max(hw eig);
hw eig = hw eig/hw max;
if ( nodd == 1) % N is odd
                                                                                                                                                                                                           % STEP 4.2 MAP EIGENVECTOR INTO:
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     hn(m+1:1:2*m) = hn(m:-1:1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          hmax = max(abs(hn));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   hn = hn / hmax;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 end & nodd
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               ich = 0;
                                                                                                                                                                                                                                                                                        9000
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  ====8
```

### FIG. SE

33

```
- METRICS J(ISI) = "errM isi" AND J(ACI) = "errM aci"
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   - SNR ERROR CONTRIBUTORS "erry isi" AND "erry aci"
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           w_vector(k_wave+1) = w_vector(k_wave+1) + hn(ii+1) * hn(ii+1+ ...
nc*k_wave);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      scale_isi_aci = 1/w_vector(1);
w_vector = w_vector * scale_isi_aci;
w_vector = w_vector * scale_isi_aci;
% normalize
errV isi = sum(w_vector(2:M) .*w_vector(2:M)); % ISI LS error
%2-sided power summation of isi residual errors
errV_isi = 2. * errV_isi;
errV_isiMax = max( abs(w_vector(2:M)) );
%====a_matrix = m+1 x 2m+1 = A
a_matrix= zeros(m+1,2*m+1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        - MATRICES "w_matrix" AND "w_f_matrix"
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       a_matrix(i_r+1, nic) = hn(nic - n_cc);
& STEP 5 WEIGHTED LS ERROR METRICS FOR:
                                                                                                                                                    err_pass = b_vector' * passband * b_vector;
err_stop = b_vector' * stopband * b_vector;
err_dead = b_vector' * deadband * b_vector;
beta_pass = alpha_1 * err_pass;
beta_stop = alpha_2 * err_stop;
beta_dead = alpha_5 * err_dead;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         - LS ERROR MATRIX "w_matrix"

- J(ISI) = "errM_isi"

- SNR LOSS ISI ERROR "errV_isi"
                                  - J(PASSBAND) = "beta_pass"
                                                              - J(STOPBAND) = "beta_stop"
- J(DEADBAND) = "beta_dead"
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    % ISI error residual vector w_vector
                                                                                                                                             for i r = 0:m

n cc = i r * nc;

if ( i r>=1 & i r<=N)

nic = (n_cc+1):(2*m+1);
                                                                                                                                                                                                                                                                                                                                                                                                                           & STEP 6 ISI AND ACI LS:
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 n_i = N - 1 - k_wave*nc;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               w vector (k \text{ wave+1}) = 0.;
                                                                                                     - J (DEADBAND)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        STEP 6.1 J(ISI):
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            for k wave = 0:M
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             for ii = 0:n i
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            end
                                                                                                                                                                                                                                                                                                                                                                                           34
```

## FIG. 5E

33

```
- MATRICES "w matrix" AND "w f matrix"
- METRICS J(ISI) = "errM isi" AND J(ACI) = "errM aci"
- SNR ERROR CONTRIBUTORS "errV isi" AND "errV aci"
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                scale isi_aci = 1/w_vector(1);
w_vector = w_vector * scale_isi_aci;
w_vector = w_vector * scale_isi_aci;
errV_isi = sum(w_vector(2:M) .*w_vector(2:M)); %ISI LS error
%2-sided power summation of isi residual errors
errV_isi = 2. * errV_isi;
errV_isiMax = max(abs(w_vector(2:M)));
%====a_matrix = m+1 x 2m+1 = A
a_matrix= zeros(m+1,2*m+1);
for i r = 0:m
n_cc = i r * nc;
if (i r>= 0:m
n_cc = i r * nc;
if (i r>= 1 r * nc;
a_matrix(i_r+1, nic) = hn(nic - n_cc);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   for ii = 0:n_i
% ISI error residual vector w_vector
w_vector(k_wave+1)=w_vector(k_wave+1)+hn(ii+1)*hn(ii+1+ ...
& STEP 5 WEIGHTED LS ERROR METRICS FOR:
                                                                                                                                        - IS ERROR MATRIX "w matrix"

- J(ISI) = "errM_isi"

- SNR LOSS ISI ERROR "errV_isi"
                                                                                                                                                            err_stop = b_vector' * passband * b_vector;
err_stop = b_vector' * stopband * b_vector;
err_dead = b_vector' * deadband * b_vector;
beta_pass = alpha_1 * err_pass;
beta_stop = alpha_2 * err_stop;
beta_dead = alpha_5 * err_dead;
                                - J(PASSBAND) = "beta_pass"
- J(STOPBAND) = "beta_stop"
- J(DEADBAND) = "beta_dead"
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        nc*k_wave);
                                                                                                                                                                                                                                                                                                                                                                                                                                        & STEP 6 ISI AND ACI LS:
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          n_1 = N - 1 - k_wave^*nc;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        w_vector(k_wave+1) = 0.;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      STEP 6.1 J(ISI):
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 for k_wave = 0:M
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          8====
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     end
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               end
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   end
                                                                                                                                                                                                                                                                                                                                                                                                     34
```

#### FIG. 5G

```
- PASSBAND RIPPLE LOSS "xloss ripple", dB - ISI LOSS "xloss isi", dB
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                明 明
                                                                                       STEP 7.1 WEIGHTED LS ERROR METRICS FOR ISI, ACI, TOTAL

- WEIGHTED ISI LS ERROR METRIC "beta_isi"

- WEIGHTED ACI LS ERROR METRIC "beta_aci"

- TOTAL LS ERROR METRIC J = "errM_LS"
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   STEP 7.3 UPDATE J LS ERROR MATRIX "PW_t" FOR NEXT ITERATION
                                                                                                                                                                                                                                                                         STEP 7.2 SAVE WEIGHTED LS ERROR METRICS FOR EACH ITERATION
                       UPDATE LS ERROR MATRIX "pw_t" FOR NEXT
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    STEP 8.1 SNR LOSSES DUE TO PASSBAND RIPPLE, ISI, ACI, AND THE TOTAL SNR LOSS
                                                                                                                                                                                                                                         errM LS = beta_pass+beta_stop+beta_dead+beta_isi+beta_aci;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            p_t = p_total+ alpha_3 * w_matrix+ alpha_4 * w_f_matrix
pw_t = bw_matrix'*p_t* bw_matrix;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              "xloss_aci".
"xloss_total",
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         k_delta = 10.^( xripple/2. /20.) - 1.;
kloss_ripple = -10. * log10( 1.0 - x_delta^2 );
#===== isi loss
- WEIGHTED LS ERROR METRICS
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          xebno = 10.^( ebno / 10.0 );
xx_isi = xebno * errV_isi ;
xloss_isi = 10. * log10(1.0 + xx_isi );
%=====
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              & STEP 8 SIGNAL-TO-NOISE SNR LOSS
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 passband ripple loss
                                                                                                                                                                                                beta_isi = alpha_3*errM_isi;
                                                                                                                                                                                                                   beta_aci = alpha_4*errM_aci;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                - ACI LOSS
- TOTAL LOSS
                                                ITERATION
                                                                                                                                                                                                                                                                                                                                        scale_err = errM_LS;
                                                                                                                                                                                                                                                                                                                        if i iteration==1
7
 8 STEP
```

#### IG. SH

```
STEP 9.1 WAVELET FREQUENCY DESIGN HARMONICS "hn_eig
                                                                                                        loss_LS =[loss_LS; i_iteration xloss_total .... xloss_rlpple xloss_isi xloss_aci];
                                                                                   STEP 8.2 SAVE SNR LOSSES FOR EACH ITERATION
                                                                                                                                                             & STEP 9 WAVELET DESIGN FOR FIG. 6
aci loss
= 10.^( x_imbal_aci / 10. );
= xebno * errV_aci * x_g_aci ;
                                                                                                                                                                                                                                                                                                                                                                                                                                                   STEP 9.2 WAVELET TIME RESPONSE "hn"
                                                                                                                                                                                                                                       'Harmonic number Harmonic value'
[(0:n_f-1)' hw_eig]
                                                                                                                                                                                                                                                                                                                                                                                                                                                                        'Sample index Wavelet response' [(0:m)' hn(m+1:2*m+1)']
                                                                                                                                       %---- end of iterations
                                                                                                                                                                                                                                                                                 0.9499
0.9842
0.98685
0.9434
0.9428
0.2428
0.2428
0.0019
0.0019
0.0000
0.0000
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       1.0000
0.9941
0.9765
0.9476
0.9080
                                                                                                                                                                                                                                                                                 1.0000
3.0000
5.0000
6.0000
7.0000
10.0000
111.0000
113.0000
115.0000
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  1.0000
2.0000
3.0000
4.0000
5.0000
          x_g_aci
xx_aci
%====
                                                                                                                            8====
                                                                                                                                                 end
```

51	0.00923 0.00923 0.00923 0.00923 0.00923 0.00923 0.00923 0.00923	00000000000000000000000000000000000000
FIG.	6.0000 111.0000 112.0000 113.0000 114.0000 115.0000 117.0000 118.0000 119.0000	2.000 2.000 3.000 3.000 4.000 6.0000 6.000 6.000 6.000 6.000 6.000 6.000 6.000 6.000 6.0

## FIG. 5J

-0.0701	.057	.049	.039	.028	.017	900.	.004	.014	.023	.030	.037	.042	.045	.046	.046	.044	.041	.037	.031	.025	.018	.011	.004	.002	.009	.015	.020	.025	.028	.031	.032	.032	.032
60.0000	2.000	3.000	4.000	5.000	6.000	7.000	8.000	0000.6	0.000	1.000	2.000	3.000	4.000	5.000	6.000	7.000	8.000	000.6	0.000	1.000	2.000	3.000	4.000	5.000	6.000	7.000	8.000	9.000	0.00	1,000	2.00	3.000	4.00

### FIG. 5K

```
0.0013
0.0006
0.0001
      0.0179
0.0168
0.0154
                        0.0138
                                    0.0103
                                                             0.0036
                                                 0.0067
0.0187
                                                       0.0051
                                                121.0000
122.0000
123.0000
124.0000
                                                                         125.0000
126.0000
127.0000
           115.0000
                        117.0000
113.0000
     114.0000
                                    119.0000
                                           120.0000
                                                                                             128.0000
```

#### 38

\*\*\*\*\*

```
HE
8 STEP 10 ITERATION CONVERGENCE IS MEASURED BY
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              legend('passband','stopband','deadband','ISI','ACI')
                                   CONVERGENCE OF THE LS ERRORS IN
                                                                                                                                                                          plot(err_LS(:,1), err_LS(:,7),'k')
legend('Total LS error relative to iteration=1')
ylabel('Total LS error relative to iteration=1')
                                                                                                                                                                                                                                                                                                                                                                                                                                                            plot(err_LS(:,1), err_LS(:,3), 'k--')
plot(err_LS(:,1), err_LS(:,4), 'k')
plot(err_LS(:,1), err_LS(:,5), 'b')
plot(err_LS(:,1), err_LS(:,6), 'b--')
title('LS ERROR CONTRIBUTORS VS. ITERATION')
                                                                                                                                                                                                                                                      xlabel('Iteration number')
title('IOTAL LS ERROR J VS. ITERATION')
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         ylabel('LS error relative to total=1')
                                                                                                                                                                                                                                                                                                                                                                                                        plot (err_LS(:,1), err_LS(:,2),'k')
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  xlabel('Iteration number')
                                                                  figure (1), figure(2)
                                                                                                                                                   figure(1)
                                                                                                                                                                                                                                                                                                                                                                                     figure(2)
                                                                                                                                                                                                                                                                                                                                                                                                                                       hold on
                                                                                                                                                                                                                                                                                                          grid on
                                                                                                                                                                                                                                                                                                                                     hold on
                                                                                                                            % plots
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               grid on
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        hold on
```

#### FIG. 5L

```
- WAVELET FILTER PERFORMANCE IN figure (3)
- WAVELET RIPPLE, ISI, ACI SNR LOSSES IN figure (4)
                                                                                                                                                                                                                                                                                            x2=length(hw_wsr);
x3=length(hw_wsr);
plot(freq(1:x2)*M,hw_ref, 'b--')
plot(freq(1:x3)*M,hw_wsr, 'b--')
legend('Wavelet response', 'pass & stop templates', 'Wavelet sample
8 STEP 11 PARAMETERS ARE SELECTED TO OPTIMIZE:
                                                                              - WAVELET TIME RESPONSE IN figure (5)
                                                                                                                                 figure(3)
plot(freq*M, hw db,'k')
axis([0 200 -100 10])
grid on
xlabel('Frequency/Wavelet sample rate')
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             plot (loss LS(:,1), loss LS(:,3), 'k--')
plot (loss_LS(:,1), loss_LS(:,4), 'b')
plot (loss_LS(:,1), loss_LS(:,5), 'b--')
title('SNR_LOSS VS. ITERATION')
legend('total', 'ripple', 'ISI','ACI')
ylabel('SNR_LOSS, dB')
xlabel('Iteration number')
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      plot(loss_LS(:,1),loss_LS(:,2),'k')
                                                                                                                                                                                                                                                                                                                                                                                                                                    title ('WAVELET FREQUENCY RESPONSE')
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 xlabel('Time/Wavelet sample rate')
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          ylabel('Wavelet time response')
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     title('WAVELET TIME RESPONSE')
                                                                                                                                                                                                                                                 ylabel('Power Spectrum, dB')
                                                                                                                                                                                                                                                                                                                                                                                                                                                           grid on
axis([0 1.4 -100 0])
hold on
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                axis([-8 8 -0.4 1])
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      plot(xx,hn','k')
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           : (w:w-)=xx
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     figure(4)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    figure(5)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  grid on
hold on
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   xx=xx/M;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               hold on
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                grid on
                                                                                                                                                                                                                                                                         hold on
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   hold on
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   hold on
                                                                                                                                                                                                                                                                                                                                                                                                               rate')
```

#### FIG. 5M

```
8 STEP 12 CALCULATION OF NEW WAVELET WAVEFORM "hn_new"
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         $ STEP 12.3 MAP WAVELET FREQUENCY DESIGN HARMONICS "hw_eig"
8 STEP 12.1 INTO NEW WAVELET IMPULSE RESPONSE IN TIME "hn_new"
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       STEP 12.2 MATRIX "bw matrix new" FOR MAPPING WAVELET FREQUENCY DESIGN HARMONICS INTO NEWWAVELET IMPULSE
                                                                                                                                                                                                                   8 STEP 12.1 WAVELET SAMPLE INTERVAL "M_new" AND LENGTH "N_new"
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  Case 2: Fix sampling and dilate M_new = 2^p M hn = hn(n - q M_new) M_new = M*(2^p);
                                                                                                                                                                                                                                                                                                                Case 1: Fix M_new = M and dilate sampling hn = hn(n 2^{-1}p - q M)
                                                                                                                                                                                                                                                                                                                                                                          = n_p for n = n_0 + n_p 2^-p
                                            - "p" SCALE (DILATION)
- "q" TRANSLATION
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            & N is odd
                                                                                                                                                                                                                                                                       8== Wavelet sample interval M_new for:
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   N is even
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       N_new = M_new*L+1; % Wavelet length
                     FOR THE PARAMETERS:
                                                                                                                      p = 2 % scale change or dilation
q = 2 % time translation
k = 3 % frequency translation
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     bw_matrix_new(l,:) = ones(l,n_f);
                                                                                       - "k" FREQUENCY
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                RESPONSE IN TIME
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                nodd= flx( N_new/2 );
nodd = N_new - 2 * nodd ;
if ( nodd == 1)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        m_{\text{new}} = (N_{\text{new}} - 1) / 2 else
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 фÞ
                                                                                                                                                                                                                                                                                                                                                    n_new = n 2^-p
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 m_new = N_new/2;
                                                                                                                                        % Wavelet parameters
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     end
```

#### FIG. 5N

```
- MOTHER WAVELET "hn"
- NEW WAVELET "hn_new" WITHOUT FREQUENCY TRANSLATION
                                                                                                                                                                  hmax 0 = max( abs(hn 0) );

$==== normalized hn 0 is new baseband Wavelet with q=k=0
hn 0 = hn 0/ hmax 0;

$==== hn 1 is hn 0 with translation in time q*M_new
for n=1:N_new+q*M_new
if n <= q*M_new
if n <= q*M_new
hn 1(n) = 0;</pre>
                                                                                                                                                                                                                                                                                                                                                                                                           for n=1:\overline{N} new+q*M new hn_new(n) = hn_1(n)*exp( i*(2*pi*k*(n-1)/(M_new*L)) );
                                                                                                                                                                                                                                                                                                                                                                                             }==== hn_new is hnl with translation in frequency by k
title('TIME RESPONSE FOR MOTHER, NEW WAVELETS')
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   STEP 12.4 PLOT WAVELET TIME RESPONSE FOR:
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             legend('MOTHER WAVELET','NEW WAVELET')
xlabel('Time/hn\_new sample rate')
ylabel('Wavelet time response')
                                                                                                                                                                                                                                                                                                                     hn_1(n) = hn_0(n-q^*M_new);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          xxi = (L/2)*(1-1/2^p)*M_new;

xx2 = (L/2)*(1+1/2^p)*M_new;

for n=1:N_new+q*M_new

if n<xxi | n>xx2

hn1(n) = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              x_n = (1:N new+q*M_new)/M_new;
x_n = x_n-L/2;
plot(x_n,hnl,'k')
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           hnl(n) = hn(n-xx1+1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         plot (x_n, hn_1, 'k--')
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              figure (6)
                                                                                                                                                                                                                                                                                                  else.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          else
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       hold on
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               hold on
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     hold on
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              end
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             grid on
                                                                                                                                                                                                                                                                                                                                         end
                                                                                                                                                                                                                                                                                                                                                                               80008
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              0000
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               end
                                                                                                                                                                                                                                                                                                                                                                                                                                                     end
                                                                                                                                                                                                                                                                                                                                                           end
```

## FIG. 50

```
arg_rot = twopi* rem( (0:N_new-1)*ich /M_new , 1 );
[freq, hw2_db] = freq_rsp(hn_0, arg_rot, n_fft);
plot(freq*M,hw2_db,'k--')
axis([0 8 -100 10])
8 STEP 12.5 PLOT WAVELET FREQUENCY RESPONSE FOR:
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              title ('POWER SPECTRUM OF MOTHER, NEW WAVELETS')
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               title('POWER SPECTRUM OF MOTHER, NEW WAVELETS')
                                                                                                                                                                                                                     arg_rot = twopi* rem( (0:N-1)*ich /nc , 1 );
[freq, hw_db] = freq_rsp(hn, arg_rot, n_fft);
plot(freq*M, hw_db,'k')
                                                                                 sample rate
                                                                                                            vs. frequency/hn_new sample rate
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           %==== plot frequency response of hn, hn_new
                                                                                                                                                                  figure(7) % vs. frequency/hn sample rate
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           xlabel('Frequency/hn\_new sample rate')
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        vs. frequency/hn_new sample rate
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    legend ('MOTHER WAVELET', 'NEW WAVELET')
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     legend ('MOTHER WAVELET', 'NEW WAVELET')
                                                   - NEW WAVELET "hn_new"
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           xlabel('Frequency/hn sample rate')
                         - MOTHER WAVELET "hn"
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          ylabel('Wavelet time response')
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            ylabel('Wavelet time response')
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                xlabel('Time/hn sample rate')
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              xlabel('Time/hn sample rate')
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               plot(freq*M_new,hw2_db,'k--')
axis([0 8 -100 10])
                                                                                 vs. frequency/hn
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     ylabel ('Power Spectrum, dB')
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     ylabel('Power Spectrum, dB')
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              plot(freg*M_new, hw_db,'k')
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  figure(8)
                                                                                                                                                                                                  ich = 0;
                                                                                                                                                                                                                                                                                                         hold on
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            hold on
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 grid on
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          hold on
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             grid on
                                                                                                                                                                                                                                                                                                                                        ich=k;
```

#### FIG. 5P

```
p_matrix(n+1,ml+1)=1./pl*(an(n+1)*an(ml+1)*(omega_u-omega_l)....
-{ an(ml+1) *ml*( sin( n*omega_u ) - sin( n*omega_l ) ) + ....
an(n+1) *n * ( sin(ml*omega_u ) - sin(ml*omega_l ) ) / ( ml*n ) + ( ....
(n+ml)* ( sin( (n-ml)*omega_u ) - sin((n-ml)*omega_l ) )...
+(n-ml)*(sin( (n+ml)*omega_u ) -sin((n+ml)*omega_l ) ...
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              p_matrix(n+1,m1+1)=1./pi*(an(m1+1)-1.)*(an(n+1)*(omega_u-omega_1)-....
(sin(n*omega_u)-sin(n*omega_1) /n );
end
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               if ( m1 ==n )
if ( n ~= 0)
p_matrix(n+1,ml+1)=1./pi*((an(n+1)*an(n+1)+0.5)*(omega_u-omega_l)-...
2.* an(n+1) * ( sin( n*omega_u )- sin( n*omega_l ) ) ...
/n + (sin(2.* n*omega_u) - sin(2.*n*omega_l))/( 4.* n) );
                                                                                                                                                                                                                                                                                                                                                  p_matrix(n,m): a nXm real, symmetry and positive-definite matrix
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         p_matrix(n+1,ml+1)=1./pi*(an(n+1)-1.)*(an(ml+1)*(omega_u-omega_l)-...
{ sin(ml*omega_u } -sin( ml*omega_l) } /ml };
end
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 p_matrix(n+1,m1+1)=1./pi*(an(n+1)-1.)*(an(n+1)-1.)*(omega_u-omega_l);
                                                                                                                                                                                                  compute the real, symmetric, and positive definite matrix input: omega_l: lower edge (radians) omega_u: upper edge (radians)
                                                               STEP 13.1 FUNCTION "pmn" COMPUTES MATRIX FOR J(BAND) IN
                                                                                                                                                                                                                                                                                                       an(.): 1xm column vector
& STEP 13 FUNCTIONS USED IN MATLAB PROGRAM
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         filter length 'N' 19 odd
                                                                                                                                                             function p_matrix= pmn(omega_l,omega_u, N,an)
                                                                                                                                                                                                                                                                                                                                                                                                                  twopi = 2. * pi;
check filter lenght is odd or even
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 N is even
                                                                                                                                                                                                                                                                                                    N: filter length,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   if (n == 0)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              1f (m1 == 0)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              end % end of ml loop
end % end of n loop
                                                                                                                                                                                                                                                                                                                                                                                                                                                                    nodd = fix(N/2);
nodd = N - 2 * nodd;
if ( nodd == 1)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            m = ( N-1) /2;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 else
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 if ( nodd == 1)
for n= 0:m
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               for ml= 0:m
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    end
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 m = N/2;
                                                                                                                                                                                                                                                                                                                                       output
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              else
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       else
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               end
```

## FIG. 52

```
p_matrix(n+1,m1+1) = 1./pi * ( ...
an(n+1) * an(m1+1) * ( omega_u - omega_l ) - ...
an(m1+1)*(sin((n+.5)*omega_u)-sin((n+.5)*omega_l))/( n + 0.5) - ...
an(n+1)*(sin((m1+.5)*omega_u)-sin((m1+.5)*omega_l))/(m1+0.5) + ...
(sin((n-m1)*omega_u) - sin((n-m1)*omega_l))/(2.* (n-m1)) + ...
(sin((n+m1+1)*omega_u)-sin((n+m1+1)*omega_l))/(2.* (n+m1+1));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  % STEP 13.2 FUNCTION "freq_rsp" COMPUTES FOURIER TRANSFORM OF
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          INPUT "hn" VS. FREQUENCY/WAVELET SAMPLE RATE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         function [freq, hw_db] = freq_rsp(hn, arg_rot, n_freq )
                                                                                                                            p_matrix(n+1,m1+1) = 1./pi * ( ...
  (an(n+1)*an(n+1) + 0.5) * ( omega_u - omega_l ) - ...
2. * an(n+1) * ( sin( (n+.5) * omega_u) - ...
  sin( (n+.5) * omega_l) )/( n + 0.5 ) + ...
  ( sin( (2*n+1) * omega_u ) -sin( (2*n+1) * omega_l ) ) ...
  /( 2. * ( 2.*n + 1) )  );
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             for nf = 1: n_freq
arg=twopi * rem( freq(nf) * ((1:n_filter) -1-m),1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   hw = sum( hn .*exp( (-arg+arg_rot)*i));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          in normalized freq interval (0., 0.5)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   hw_max = max( abs(hw_mag) );
hw_mag = hw_mag /hw_max;
hw_db = 20.** log10( hw_mag+ 1.e-20);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        & Fourier transform of input hn
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            end % end of m1 loop
end % end of n loop
l % end of if nodd =1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  hw_mag(nf) = abs(hw);
when N is even
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             % n_freq # of frequency twopi = 2. * pi;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            df = 0.5/ (n_freq -1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                n filter = length(hn);
                                                                                      if ( m1 == n )
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                % frequency response
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            m=(n_filter-1)/2;
freq = (0:df:0.5);
                                                         for m1 = 0:m-1
                            for n = 0:m-1
  end
```

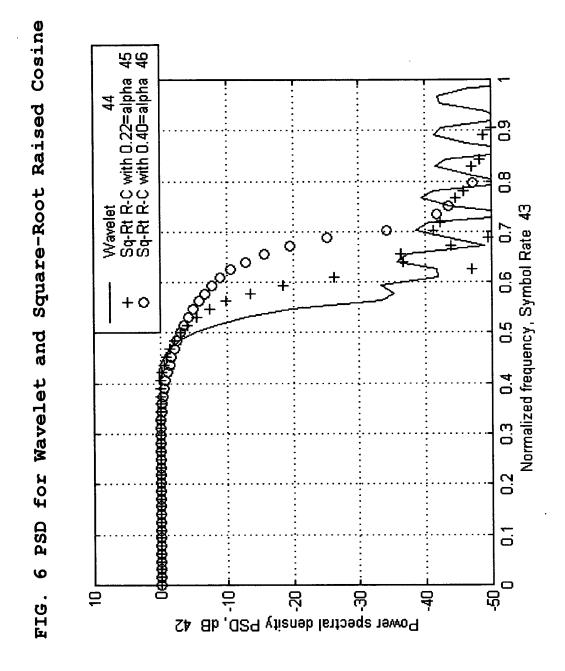
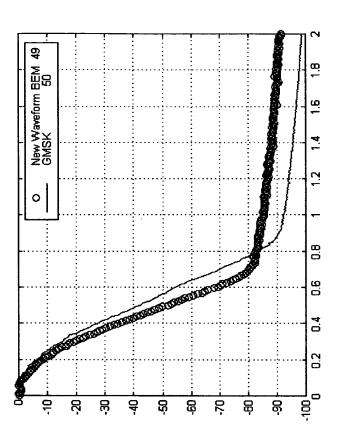


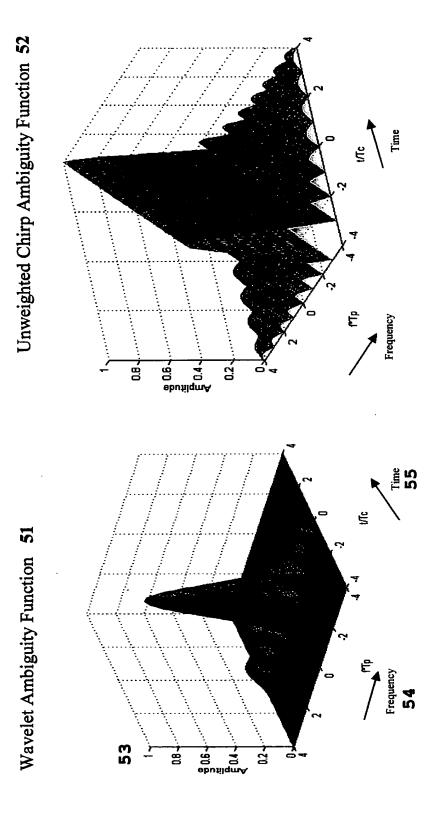
FIG. 7 PSD for New Waveform BEM and GMSK



Normalized frequency, bit rate 48

Power spectral density PSD, dB 47

Radar Ambiguity Functions of Wavelet and Unweighted Chirp Waveform ω FIG.



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